

**Trig Functions:**

$$\sin(x) = \frac{\text{opposite}}{\text{hypotenuse}}$$

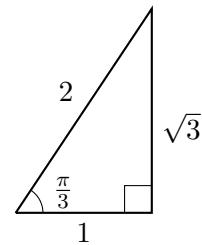
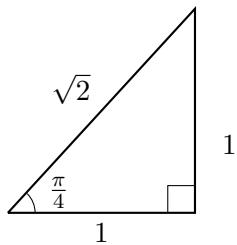
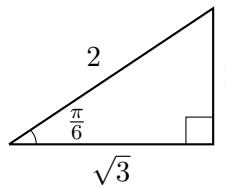
$$\cos(x) = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan(x) = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sec(x) = \frac{\text{hypotenuse}}{\text{adjacent}}$$

$$\csc(x) = \frac{\text{hypotenuse}}{\text{opposite}}$$

$$\cot(x) = \frac{\text{adjacent}}{\text{opposite}}$$

**Standard Triangles:****Trig Identities:**

- Other 4 trig functions written in terms of  $\sin(x)$  &  $\cos(x)$

$$\tan(x) = \frac{\sin(x)}{\cos(x)}$$

$$\sec(x) = \frac{1}{\cos(x)}$$

$$\csc(x) = \frac{1}{\sin(x)}$$

$$\cot(x) = \frac{\cos(x)}{\sin(x)}$$

- Pythagorean identities

$$\sin^2(x) + \cos^2(x) = 1$$

$$\tan^2(x) + 1 = \sec^2(x)$$

$$1 + \cot^2(x) = \csc^2(x)$$

- Double angle identities

$$\sin(2x) = 2 \sin(x) \cos(x)$$

$$\cos(2x) = \cos^2(x) - \sin^2(x)$$

- Power reducing identities

$$\sin^2(x) = \frac{(1 - \cos(2x))}{2}$$

$$\cos^2(x) = \frac{(1 + \cos(2x))}{2}$$

You can derive the power reducing identities from the double angle identity for cosine:

$$\cos(2x) = \cos^2 x - \sin^2 x$$

If you want the identity involving  $\sin^2(x)$ , replace  $\cos^2(x)$  with  $1 - \sin^2(x)$ .

$$\begin{aligned}\cos(2x) &= \cos^2 x - \sin^2 x \\ &= (1 - \sin^2 x) - \sin^2 x \\ &= 1 - 2 \sin^2 x\end{aligned}$$

Solve for  $\sin^2 x$ :

$$\begin{aligned}\cos(2x) &= 1 - 2 \sin^2 x \\ 2 \sin^2 x &= 1 - \cos(2x) \\ \sin^2 x &= \frac{1 - \cos(2x)}{2}\end{aligned}$$

If you want the identity involving  $\cos^2(x)$ , replace  $\sin^2(x)$  with  $1 - \cos^2(x)$  and follow a similar process.